

## Midterm Studyguide

Date \_\_\_\_\_ Period \_\_\_\_\_

**Simplify.**

1)  $\frac{2}{-2i}$

- A)  $\frac{3i}{2}$   
 B)  $i$   
 C)  $2i$   
 D)  $-\frac{i}{2}$

2)  $\frac{3}{-10i}$

- A)  $\frac{i}{2}$   
 B)  $\frac{3i}{13}$   
 C)  $\frac{i}{4}$   
 D)  $\frac{3i}{10}$

3)  $\frac{2}{\sqrt{5} + 5\sqrt{3}}$

- A)  $\frac{-\sqrt{5} + 5\sqrt{3}}{35}$   
 B)  $\frac{-\sqrt{5} + 5}{38}$   
 C)  $\frac{-\sqrt{6} + 8\sqrt{3}}{93}$   
 D)  $\frac{-4\sqrt{6} + 20\sqrt{3}}{69}$

4)  $(2i)(2i)(1 - 8i)$

- A)  $-4 + 32i$   
 B)  $-32i$   
 C)  $4 - 32i$   
 D)  $4 + 32i$

5)  $(-1 + 3i)^2$

- A)  $-8 + 6i$   
 B)  $-8 - 6i$   
 C)  $-18i$   
 D)  $9$

6)  $(3i) + (-6 + 8i) - (7i)$

- A)  $-6 + 4i$   
 B)  $-6 - 2i$   
 C)  $-6 + 18i$   
 D)  $6 - 12i$

7)  $(-7 + 7i)^2$

- A)  $32 - 126i$   
 B)  $98i$   
 C)  $-98i$   
 D)  $4$

8)  $\frac{7i}{7 - 4i}$

- A)  $\frac{35i - 28}{41}$   
 B)  $\frac{14 + 8i}{13}$   
 C)  $\frac{49i - 28}{65}$   
 D)  $\frac{14i - 7}{20}$

9)  $\frac{4i}{-2 - 7i}$

- A)  $\frac{-8i - 28}{53}$   
 B)  $\frac{-3 + 21i}{25}$   
 C)  $\frac{-2i - 14}{25}$   
 D)  $\frac{-14 + 49i}{53}$

**Solve each equation by factoring.**

10)  $x^2 - 21 = -4x$

- A)  $\{3, -8\}$       B)  $\{5, 6\}$   
C)  $\{-7, -1\}$       D)  $\{3, -7\}$

11)  $3r^2 + 25r + 28 = 0$

- A)  $\left\{-\frac{4}{3}, 4\right\}$       B)  $\left\{\frac{1}{2}, -\frac{4}{5}\right\}$   
C)  $\left\{\frac{4}{3}, 7\right\}$       D)  $\left\{-\frac{4}{3}, -7\right\}$

**Solve each equation by taking square roots.**

12)  $3v^2 + 3 = -43$

- A)  $\left\{\frac{2i\sqrt{30}}{3}\right\}$   
B)  $\left\{\frac{i\sqrt{138}}{3}, -\frac{i\sqrt{138}}{3}\right\}$   
C)  $\left\{\frac{2i\sqrt{30}}{3}, -\frac{2i\sqrt{30}}{3}\right\}$   
D)  $\left\{-\frac{46}{3}, \frac{46}{3}\right\}$

**Solve each equation with the quadratic formula.**

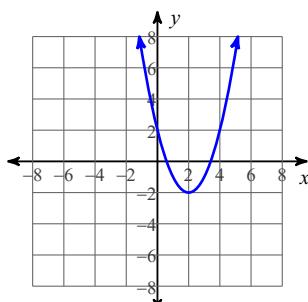
13)  $x^2 - 7 = 0$

- A)  $\left\{\frac{5}{2}, -8\right\}$       B)  $\left\{\frac{14}{3}, -6\right\}$   
C)  $\{\sqrt{7}, -\sqrt{7}\}$       D)  $\left\{1, -\frac{7}{6}\right\}$

**Identify the vertex and axis of symmetry of each. Then sketch the graph.**

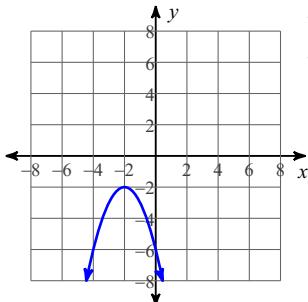
14)  $y = x^2 + 4x + 2$

A)



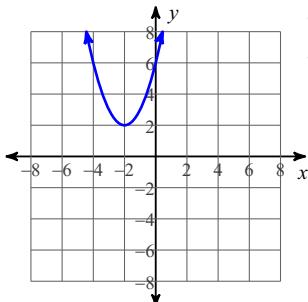
Vertex: (2, -2)  
Axis of Sym.:  $x = 2$

B)



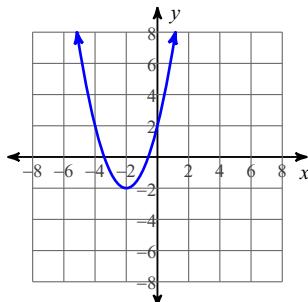
Vertex: (-2, -2)  
Axis of Sym.:  $x = -2$

C)



Vertex: (-2, 2)  
Axis of Sym.:  $x = -2$

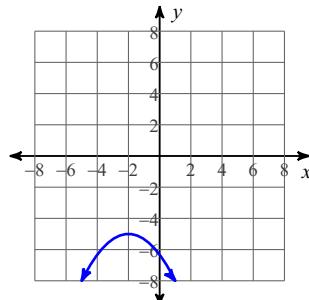
D)



Vertex: (-2, -2)  
Axis of Sym.:  $x = -2$

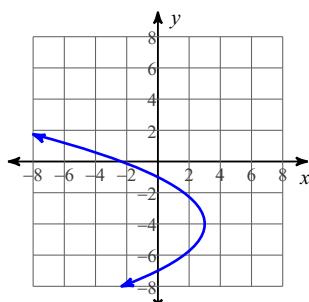
15)  $f(x) = -\frac{1}{3}x^2 + \frac{10}{3}x - \frac{31}{3}$

A)



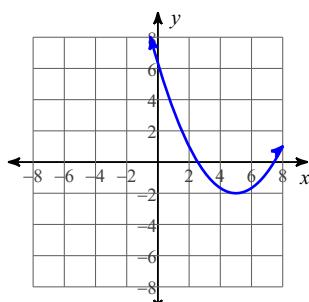
Vertex: (-2, -5)  
Axis of Sym.:  $x = -2$

B)



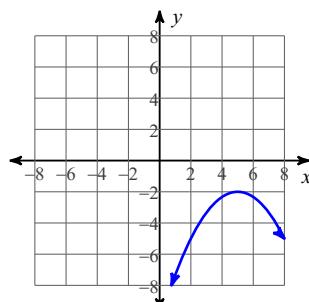
Vertex: (3, -4)  
Axis of Sym.:  $y = -4$

C)



Vertex: (5, -2)  
Axis of Sym.:  $x = 5$

D)

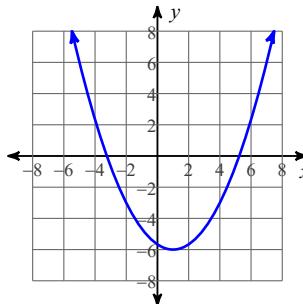


Vertex: (5, -2)  
Axis of Sym.:  $x = 5$

**Identify the vertex and focus of each. Then sketch the graph.**

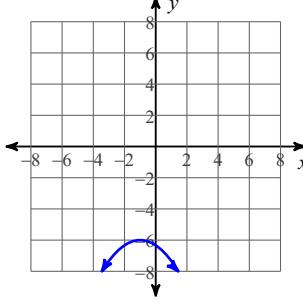
16)  $y = -\frac{1}{3}x^2 - \frac{2}{3}x - \frac{19}{3}$

A)



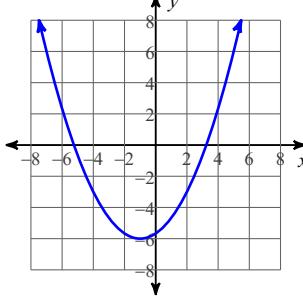
Vertex:  $(1, -6)$   
Focus:  $\left(1, -\frac{21}{4}\right)$

B)



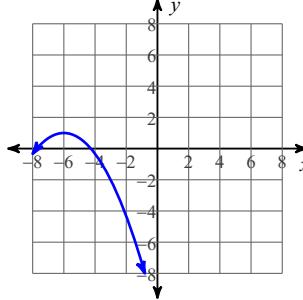
Vertex:  $(-1, -6)$   
Focus:  $\left(-1, -\frac{27}{4}\right)$

C)



Vertex:  $(-1, -6)$   
Focus:  $\left(-1, -\frac{21}{4}\right)$

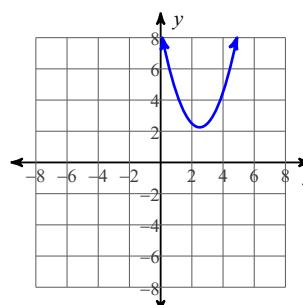
D)



Vertex:  $(-6, 1)$   
Focus:  $\left(-6, \frac{1}{4}\right)$

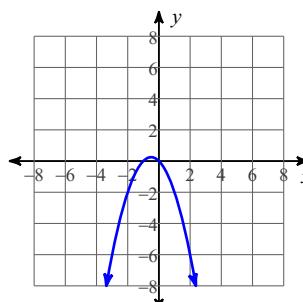
17)  $y = -(x - 4)(x - 1)$

A)



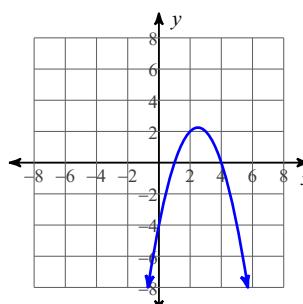
Vertex:  $\left(\frac{5}{2}, \frac{9}{4}\right)$   
Focus:  $\left(\frac{5}{2}, 2\right)$

B)



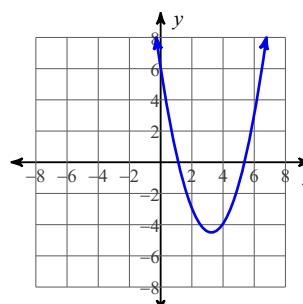
Vertex:  $\left(-\frac{1}{2}, \frac{1}{4}\right)$   
Focus:  $\left(-\frac{1}{2}, 0\right)$

C)



Vertex:  $\left(\frac{5}{2}, \frac{9}{4}\right)$   
Focus:  $\left(\frac{5}{2}, 2\right)$

D)



Vertex:  $\left(\frac{13}{4}, -\frac{9}{2}\right)$   
Focus:  $\left(\frac{13}{4}, -\frac{17}{4}\right)$

**Identify the min/max value, y-intercept, and x-intercepts of each.**

18)  $y = -2x^2 + 20x - 51$

- A) Min value = 5  
y-int: 6  
x-int: None
- B) Min value = -3  
y-int: 69  
x-int:  $\frac{12 + \sqrt{6}}{2}$  and  $\frac{12 - \sqrt{6}}{2}$
- C) Min value = -1  
y-int: 49  
x-int:  $\frac{10 + \sqrt{2}}{2}$  and  $\frac{10 - \sqrt{2}}{2}$
- D) Max value = -1  
y-int: -51  
x-int: None

20)  $y = \frac{1}{2}x(x - 9)$

- A) Min value =  $\frac{81}{8}$   
y-int:  $\frac{81}{4}$   
x-int: None
- B) Max value =  $-\frac{9}{2}$   
y-int:  $-\frac{7137}{128}$   
x-int: None
- C) Min value =  $\frac{65}{8}$   
y-int:  $\frac{117}{4}$   
x-int: None
- D) Min value =  $-\frac{81}{8}$   
y-int: 0  
x-int: 0 and 9

19)  $y = -(x + 2)^2 + 49$

- A) Min value = 49  
y-int: 53  
x-int: None
- B) Max value = -49  
y-int: -53  
x-int: None
- C) Max value = 49  
y-int: 45  
x-int: 5 and -9
- D) Max value = -2  
y-int: -2403  
x-int: None

**Factor each completely by grouping.**

21)  $9x^3 + 15x^2 + 12x + 20$

- A)  $(3x^2 + 4)(3x^2 - 5)$   
B)  $(3x^2 - 4)(3x - 5)$   
C)  $(3x^2 + 4)(3x - 4)$   
D)  $(3x^2 + 4)(3x + 5)$

22)  $2n^3 + 2n^2 + 5n + 5$

- A)  $(2n^2 - 5)(n + 1)$   
B)  $(2n^2 + 5)(n + 1)$   
C)  $(2n^2 + 5)(n - 1)$   
D)  $(2n^2 - 5)(n - 1)$

**Factor out a monomial.**

23)  $y = x^3 - 4x^2 + 3x$

- A)  $y = x(x - 1)(x - 3)$
- B)  $y = x(x - 1)(2x - 3)$
- C)  $y = x(x - 1)(x + 4)$
- D)  $y = x(x + 3)(2x - 3)$

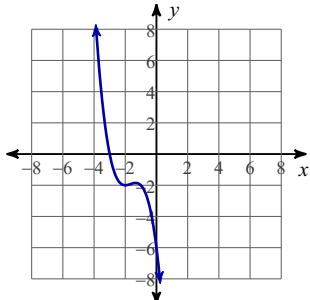
24)  $y = x^3 - x^2 - 2x$

- A)  $y = x(x + 1)(x - 2)$
- B)  $y = 3x(x + 1)(x - 2)$
- C)  $y = x(2x + 1)(x - 2)$
- D)  $y = x(x + 1)^2$

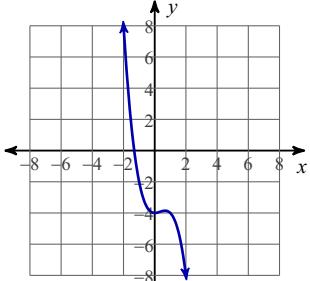
**Sketch the graph of each function.**

25)  $f(x) = -x^3 + x^2 - 4$

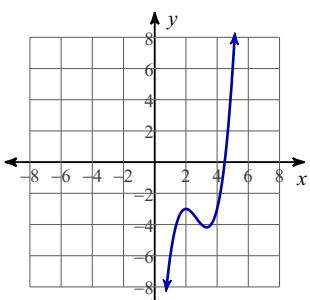
A)



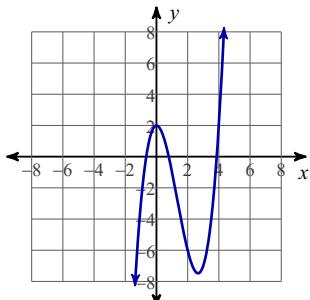
B)



C)

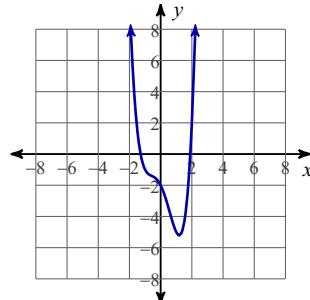


D)

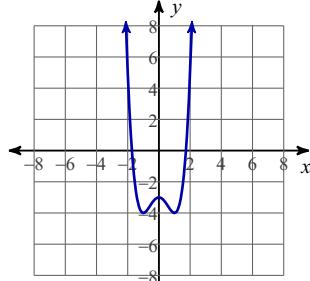


26)  $f(x) = x^4 - 2x^2 - 2x - 2$

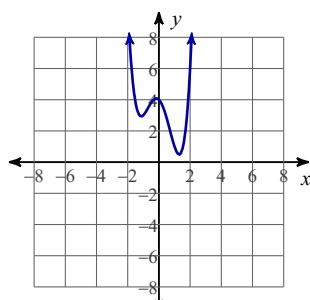
A)



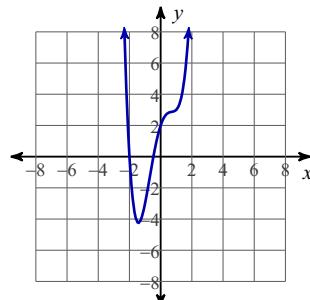
B)



C)



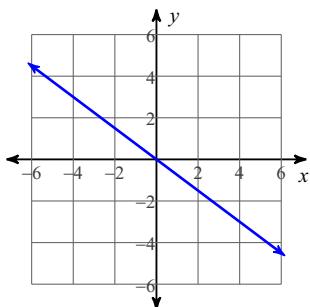
D)



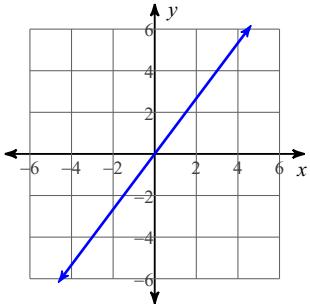
**Sketch the graph of each line.**

27)  $0 = 12y + 9x$

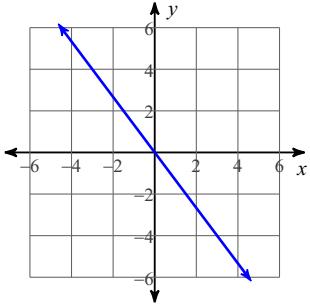
A)



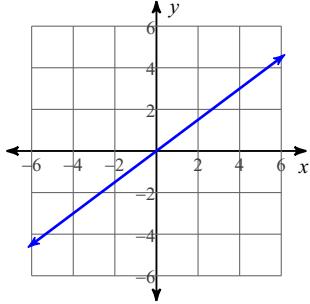
B)



C)



D)



**Find each product.**

28)  $(x - 5)(x^2 - 5x + 2)$

- A)  $x^3 - 10x^2 + 27x - 10$
- B)  $9x^3 - 9x^2 - 19x - 5$
- C)  $4x^3 + 15 - 19x$
- D)  $15x^3 + 56x^2 + 64x + 21$

**Simplify each sum.**

29)  $(2 - 3r^2 - r^4) + (4r^4 - 8r^2 - 8)$

- A)  $3r^4 - 3r^2 - 6$
- B)  $3r^4 - 11r^2 - 11$
- C)  $3r^4 - 3r^2 - 11$
- D)  $3r^4 - 11r^2 - 6$

**Simplify each difference.**

30)  $(m^4 - 4m^2 - m^3) - (3m^2 - 8m^3 - 4m^4)$

- A)  $5m^4 + 7m^3 - 14m^2$
- B)  $5m^4 + 7m^3 - 7m^2$
- C)  $5m^4 + 13m^3 - 14m^2$
- D)  $3m^4 + 13m^3 - 14m^2$

## Answers to Midterm Studyguide (ID: 1)

- |       |       |       |       |
|-------|-------|-------|-------|
| 1) B  | 2) D  | 3) A  | 4) A  |
| 5) B  | 6) A  | 7) C  | 8) C  |
| 9) A  | 10) D | 11) D | 12) B |
| 13) C | 14) D | 15) D | 16) B |
| 17) C | 18) D | 19) C | 20) D |
| 21) D | 22) B | 23) A | 24) A |
| 25) B | 26) A | 27) A | 28) A |
| 29) D | 30) B |       |       |